

# Maths Facts







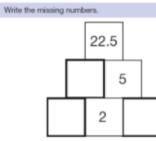
#### **Example SATs questions**

4

4

#### Here is a number pyramid.

The number in a box is the product of the two numbers below it.

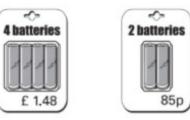


A shop sells batteries in packs of four and packs of two.

This table shows the heights of three mountains.

| Mountain          | Height in metres |
|-------------------|------------------|
| Mount Everest     | 8,848            |
| Mount Kilimanjaro | 5,895            |
| Ben Nevis         | 1,344            |

How much higher is Mount Everest than the combined height of the other two mountains?



Simon and Nick want two batteries each.

They buy a pack of four and share the cost equally.

How much does each pay?

÷

£ 1.48

This table shows the number of people living in various towns in England.

| Town    | Population |
|---------|------------|
| Bedford | 82,448     |
| Carlton | 48,493     |
| Dover   | 34,087     |
| Formby  | 24,478     |
| Telford | 166,640    |

What is the total of the numbers of people living in Formby and in Telford?

What is the difference between the numbers of people living in Bedford and in Dover?

# 4 Operations Key Language

| +                 | -                          |
|-------------------|----------------------------|
| Sum               | Less                       |
| Find the sum of   | Less than                  |
| Plus              | Leave                      |
| Total             | Difference                 |
| Find the total of | Find the difference        |
| Add               | What is the difference be- |
| More than         | tween                      |
| Make              | Minus                      |
| Addition          | Subtract                   |
| Altogether        | Take away                  |
| Together          | Take from                  |
| And               | Fewer                      |
| More than         | Left                       |
| Total             | How much more              |
| Cobined           |                            |
|                   |                            |

# Х

Multiply product Groups of Lots of Multiplication Multiplied by Times Multiple of Repeated addition ÷

Divide

Divided by

Divided into

Divided equally

Share equally

Share

Equal groups of

=

Equal to Equals The same as

### **Times Tables**

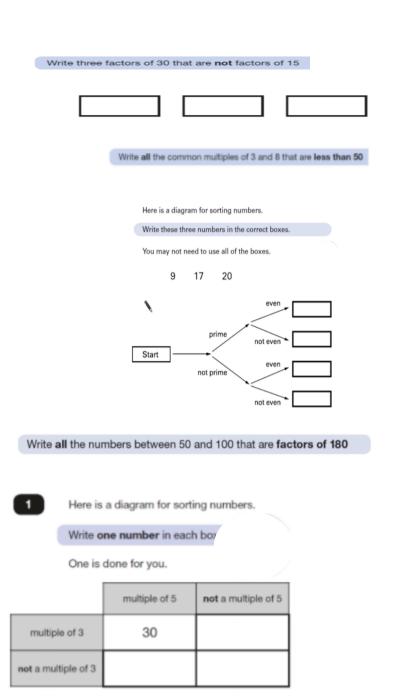
A strong knowledge of your times tables and their related division facts is essential for maths. They should be practised regularly and should be learnt out of order for easy re-call. These can be practised via TT Rockstars.

| Х  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9   | 10  | 11  | 12  |
|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|
| 1  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9   | 10  | 11  | 12  |
| 2  | 2  | 4  | 6  | 8  | 10 | 12 | 14 | 16 | 18  | 20  | 22  | 24  |
| 3  | 3  | 6  | 9  | 12 | 15 | 18 | 21 | 24 | 27  | 30  | 33  | 36  |
| 4  | 4  | 8  | 12 | 16 | 20 | 24 | 28 | 32 | 36  | 40  | 44  | 48  |
| 5  | 5  | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45  | 50  | 55  | 60  |
| 6  | 6  | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54  | 60  | 66  | 72  |
| 7  | 7  | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63  | 70  | 77  | 84  |
| 8  | 8  | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72  | 80  | 88  | 96  |
| 9  | 9  | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81  | 90  | 99  | 108 |
| 10 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90  | 100 | 110 | 120 |
| 11 | 11 | 22 | 33 | 44 | 55 | 66 | 77 | 88 | 99  | 110 | 121 | 132 |
| 12 | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 |

Learning by rote is a popular way for children to recall their times table. The following link is on Youtube and has been popular with our Year 6 children.

https://www.youtube.com/watch?v=jf2BHuSbt\_Y Alternatively, type in 'Year 3 Rolling Numbers.'





**Example SATs questions** 

#### **Factors and Multiples**

Factors are all the numbers which, when multiplied together in pairs, produce the original number. i.e.

The factors of 12 are:

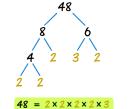
1 and 12 (1x12=12) 2 and 6 (2x6=12) 3 and 4 (3x4=12)

Numbers which have only one pair of factors (1 and itself) are known as prime numbers: 17 is prime number because the only pair of factors are 1 and 17.

Common factors—these are numbers which are factors for two different numbers i.e. the common factors of 12 and 20 are 1, 2 and 4 because these number divide exactly into both original numbers. This is important when working with fractions.

Prime factors are the factors of a given number which, when taken to its full extent, are prime. They can be shown as a prime factor tree and, when all of them are multiplied together, they will produce the original number.

Tip: Factors are always the number or smaller Multiples are always the number or bigger.



#### **Multiples**

Multiples are effectively extended times tables. The multiples of any number are the numbers into which the original number can be divided exactly. For example:

The multiples of 2 are 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30 and any other number which can be divided by 2.

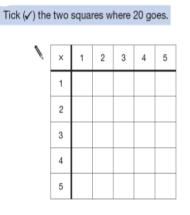
The multiples of 5 are 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80 and any other number which can be divided by 5.

Common multiples are the multiples which apply to two different numbers. I.E. the common multiples for 3 and 4 below 30 are:

312 and 24 as these are multiples for both 3 and 4.

# Example SATs questions

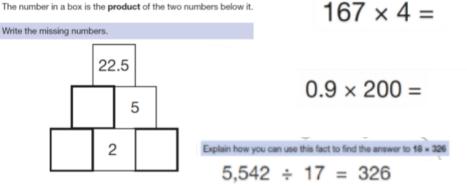
Write the missing numbers to make this multiplication grid correct. × 9 63 54 56 48



The number 20 goes in two of the squares of this multiplication grid.

Here is a number pyramid.

The number in a box is the product of the two numbers below it.



A group of friends earns £80 by washing cars.

 $581 \div 7 =$ 

They share the money equally.

They get £16 each.

How many friends are in the group?

# <u>Time</u>

#### Simple Facts

#### Months of the Year (in order)

- 60 seconds in a minute
- 60 minutes in an hour
- 24 hours in a day (12 hours in half a day)
- 7 days a weeks
- 52 weeks in a year
- 4 weeks in a month (roughly)
- 365 days in a year
- 366 days in a leap year (once every four years)
- In a leap year February has one additional day.

30 days hath September, April, June and November All the rest have 31, Except for February alone, Which has 28 days clear, And 29 in each leap year.

| 12 Midnight = 00.00 |
|---------------------|
| 1 am = 01.00        |
| 2am = 02.00         |
| 3am = -3.00         |
| 4am = 04.00         |
| 5am = 05.00         |
| 6am = 06.00         |
| 7am = 07.00         |
| 8am = 08.00         |
| 9am = 09.00         |
| 10am= 10.00         |
| 11am = 11.00        |

January February March April May June July August September October November December

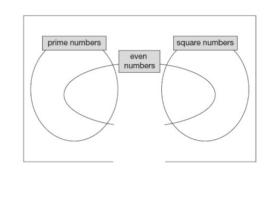
Purchasing analogue watch for your child can be extremely helpful for them to learn the time. Often, children can read digital time but cannot convert this knowledge when looking at an analogue clock in their everyday life.

12 Noon / midday = 12.00 1pm = 13.00 2pm = 14.00 3pm = 15.00 4pm = 16.00 5pm = 17.00 6pm = 18.00 7pm = 19.00 8pm = 20.00 9pm = 21.00 10pm = 22.00 11pm = 23.00

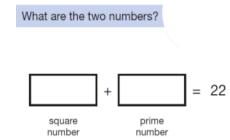
# Examples of SATs questions

Write each number in its correct place on the diagram.

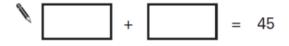
16 17 18 19



18 A square number and a prime number have a total of 22



#### Find two square numbers that total 45



#### Here is a sorting diagram for numbers.

| Write a number <b>less than 100</b> in each space. |      |          |  |  |  |
|--|------|----------|--|--|--|
|  | even | not even |  |  |  |
| a square number                                    |      |          |  |  |  |
| not a square number                                |      |          |  |  |  |

# Squares, Cubes and Primes

Square numbers are the result when a root number is multiplied by itself i.e. 5 squared  $(5^2)$  is 5x5 = 25. 25 is a square number.

Cube numbers are the result of a root number being multiplied byt itself and the answer being multiplied byt the root number again i.e 5 cubed  $(5^3)$  is 5x5x5 = 125

| Root number | Squared | Cubed |
|-------------|---------|-------|
| 1           | 1       | 1     |
| 2           | 4       | 8     |
| 3           | 9       | 27    |
| 4           | 16      | 64    |
| 5           | 25      | 125   |
| 6           | 36      | 216   |
| 7           | 49      | 343   |
| 8           | 64      | 512   |
| 9           | 81      | 729   |
| 10          | 100     | 1000  |
| 11          | 121     | 1331  |
| 12          | 144     | 1728  |

Prime numbers are those numbers which only have 1 and itself as factors.

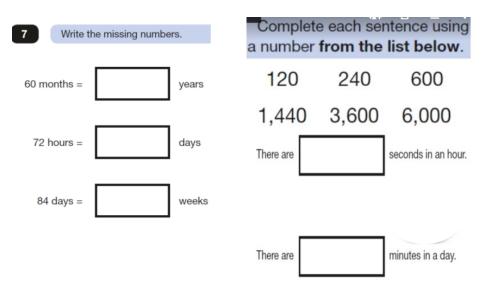
2 is the only even prime number.

1 is not a prime number.

Prime Numbers are infinite but the primes below 100 are:

2, 3, 5, 7, 11, 13, 17, 23, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

### Example SATs time questions:





Here is part of the bus timetable from Riverdale to Mott Haven.

| Riverdale   | 10:02 | 10:12 | 10:31 | 10:48 | How many minutes does it take the 10:31 bus from Riverdale to reach Mott Haven? |
|-------------|-------|-------|-------|-------|---|
| Kingsbridge | 10:11 | 10:21 | 10:38 | 10:55 | minutes   |
| Fordham     | 10:28 | 10:38 | 10:54 | 11:11 | Mr Evans is at Fordham at 10:30   |
| Tremont     | 10:36 | 10:44 | 11:00 | 11:17 | What is the <b>earliest</b> time he can reach Tremont on the bus?               |
| Mott Haven  | 10:53 | 11:01 | 11:17 | 11:34 |   |

# What is 444 minutes in hours and minutes?



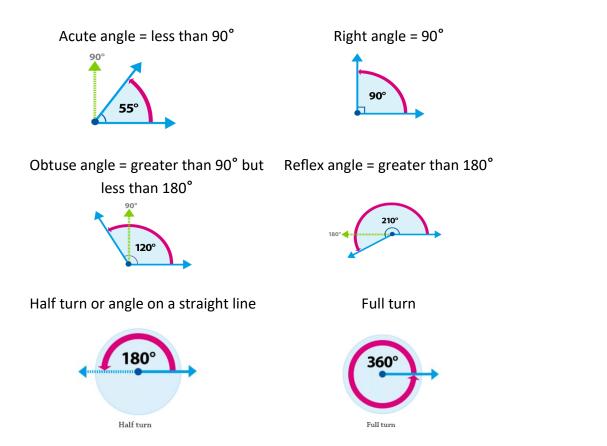
minutes

# <u>Angles</u>

# • The angles on a straight line add up to 180°

- The angles around a point add up to 360°
- Internal angles of a triangle add up to 180°
- The angles of a quadrilateral add up to 360°
- Other 2d shapes—for every additional angle add a further 180° (Pentagon, 5 angles = 360° +180° = 540°, hexagon, 6 angles = 540° + 180° = 720°, and so on) The formula (n-2) x 180 can be used to calculate the interior angles

of any regular shape (n= the number of sides on the shape)



|        | to the nearest 100                |
|--------|-----------------------------------|
|        | rounded to the<br>nearest hundred |
| 316    | 300                               |
| 3162   |                                   |
| 31628  |                                   |
| 316281 |                                   |

Amy chooses two of these cards.

| 11  | 23 | 33 | 43 |
|-----|----|----|----|
| 111 | 23 | 33 | 43 |

She adds the numbers on her two cards together. She rounds the result to the nearest 10

Her answer is 60

Which two cards did Amy choose?



Write in the missing numbers.

| Number | Rounded to the<br>nearest <b>whole</b> number |
|--------|---|
| 5.05   |   |
| 5.55   |   |
| 4.45   |   |
| 4.54   |   |

# Example SATs questions

Complete this table to show the numbers

### Rounding

Rounding is skill which can be extremely useful when estimating answers to complex calculations but it also a skill tested within SATs papers.

| ΤН | Н | Т | U | . ths |
|----|---|---|---|-------|
| 2  | 4 | 6 | 5 | . 9   |

To round to the nearest ten first we must look at the tens column. We have 6 tens so we know the number will either round up to 2470 or down to 2460. Next we must look in the units column. If it is 5 or more then we round up, if it is 4 or less we round down. As 5 is in the units, we round up to 2470.

This procedure follows for rounding to nearest thousand, hundred, unit, or tenth. The only thing that alters is the column we look in so:

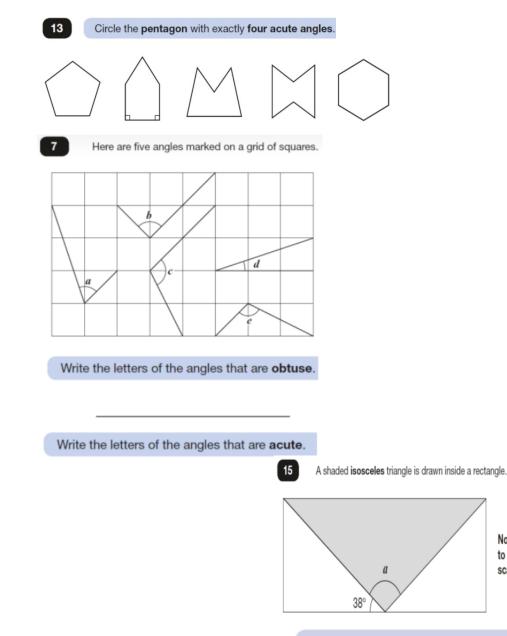
2465.9 rounded is:

2000—to the nearest thousand 2500—to the nearest hundred 2470—to the nearest ten 2455—to the nearest unit

Rounding to the nearest tenth/hundredth. Example:

**3.456** rounded to 2 decimal places/nearest hundredth = 3.46

3.456 round to 1 decimal place/nearest tenth = 3.5



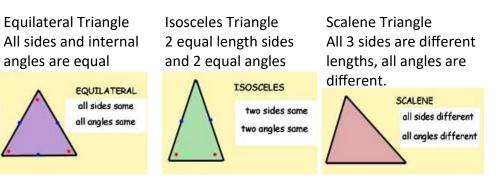
Calculate the size of angle *a*.

Not to

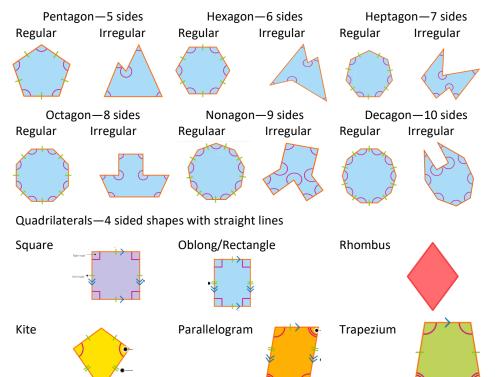
scale

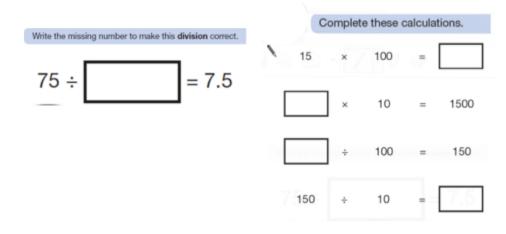
# 2d Shape

# **Example SATs questions**



Regular shapes - shapes which have equal length sides and equal angles Irregular Shapes—shapes which have unequal length sides and unequal angles.

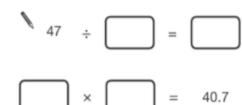




Here are five number cards.

| 0.47 | 10 | 100 | 1000 | 4.07 |
|------|----|-----|------|------|
|      |    |     |      |      |

Use four of the cards to complete these calculations.



 $2,345 \times 1,000 =$ 

### Place Value and multiplying/dividing by 10, 100 and 1000

| ТМ                  | М        | НТН                               | TTH                       | TH             | Н            | Т    | U              |                              | ths    | hths            | thths            |
|---------------------|----------|-----------------------------------|---------------------------|----------------|--------------|------|----------------|------------------------------|--------|-----------------|------------------|
| Tens of<br>Millions | Millions | Hun-<br>dred of<br>Thou-<br>sands | Tens of<br>Thou-<br>sands | Thou-<br>sands | Hun-<br>dred | Tens | Units/<br>Ones | Dec<br>ima<br>I<br>Poi<br>nt | Tenths | Hun-<br>dredths | thou-<br>sandths |
| 4                   | 2        | 7                                 | 5                         | 6              | 4            | 6    | 2              |                              | 5      | 4               | 3                |

Forty-Two million, seven hundred and fifty-six thousand four hundred and sixty-two point five four three

Multiplying by 10, 100 and 1000—count the zeroes then move the digits the same number of places to the left. The decimal point DOES NOT MOVE it is a fixed point. Gaps are plugged with a zero (you do not ADD a zero—ever!).

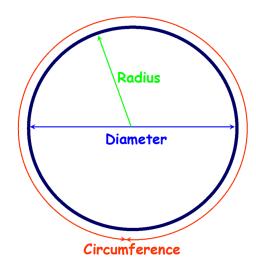
|       |   |   |   | 4 | 5 | 3 | • | 6 |  |
|-------|---|---|---|---|---|---|---|---|--|
| X10   |   |   | 4 | 5 | 3 | 6 |   |   |  |
| X100  |   | 4 | 5 | 3 | 6 | 0 |   |   |  |
| x1000 | 4 | 5 | 3 | 6 | 0 | 0 |   |   |  |

Dividing by 10, 100 and 1000—count the zeroes the move the digits the same number of places to the right. The decimal point DOES NOT MOVE it is a fixed point. Gaps are plugged with a zero.

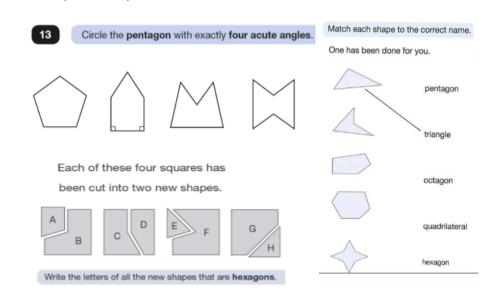
|      |  |  | 4 | 5 | 3 |   |   |   |   |
|------|--|--|---|---|---|---|---|---|---|
| ÷10  |  |  |   | 4 | 5 | • | 3 |   |   |
| ÷100 |  |  |   |   | 4 | • | 5 | 3 |   |
| ÷100 |  |  |   |   | 0 | • | 4 | 5 | 3 |

These facts can then be used to help with other calculations i.e. 50 x 70

| 5 x 7 = 35     |
|----------------|
| 50 x 7 = 350   |
| 50 x 70 = 3500 |



# Example SATs questions



A bicycle wheel has a diameter of 64 cm.

What is the radius of the bicycle wheel?

#### Circle

Circumference—the distance around the outside of the circle (it's perimeter).

Diameter—the width of the circle crossing the centre from one side to the other.

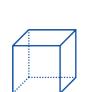
Radius—the distance from the centre of the circle to

# 3d Shape

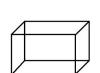
Cylinder

Pentagonal based

pyramid



Cube



Square based pyr-

Cuboid

amid

Sphere



Triangular Based Pyramid





Hexagonal prism





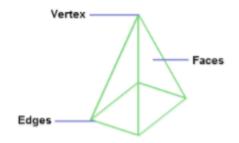
Hemisphere



Octahedron

Cone

**Triangular** Prism



Vertex—the 'corners' of the shape.

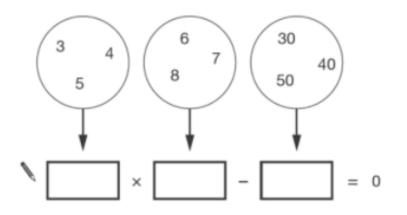
Face—the side of the shape

Edge—the joint of two faces

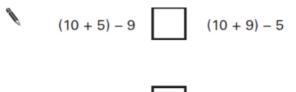
Example SATs questions

$$3^2 + 10 = 50 + (36 \div 6) =$$
  
 $20 - 4 \times 2 =$ 

Write one number from each circle to make this calculation correct.



Write the correct sign >, < or = in each of the following.



 $3 \times (4 + 5)$  $(3 \times 4) + 5$ 

10 × (4 ÷ 2) (10 × 4) ÷ 2

#### BODMAS

BODMAS is the order in which operations within a calculation must be completed.

B = Brackets
O/I= Orders (also known as powers)/ Indices
D = Division
M = Multiplication
A = Addition
S = Subtraction

 $7^2 \times 2 - (6 + 3) =$ 

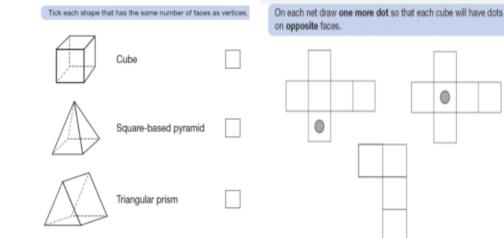
Brackets first— 6 + 3 = 9Orders/indices second— $7^2 = 49$ Division/Multiplication next— $49 \times 2 = 98$ Addition/Subtraction last—98 - 9 = 89

You might not see all the BODMAS steps in one questions so you just need to figure which step must come first, for example:

### 60-42÷6 =

If completed in left to right order the answer would be 3—this is IN-CORRECT!

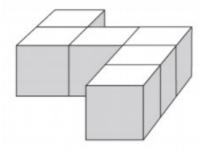
Under BODMAS 42  $\div$ 6 must be completed first (42 $\div$ 6 = 7) then this answer taken away from 60 so the CORRECT answer is 53.



Emily has 6 cubes.

Triangular-based pyramid

She sticks them together to make this model.



She paints the sides of the model grey all the way round.

She leaves the top and the bottom of the model white.

How many of the cubes in the model have **exactly two** faces painted grey?

#### **Example SATs questions**

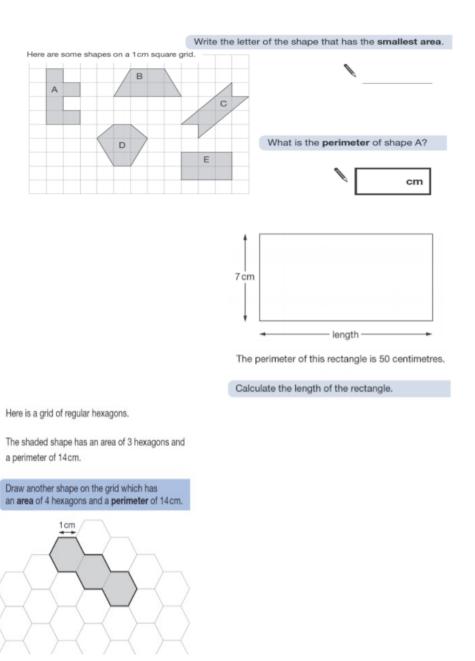
Here are diagrams of some 3-D shapes.

#### Fractions, Decimals and Percentages

Fractions, decimals and percentages can be easily converted through the methods we have taught you at school but some of them need to be remembered to help with speed during tests. This is especially helpful when ordering a mixture of fractions, decimals and percentages.

| Fraction | Decimal | Percentage |
|----------|---------|------------|
| 1/2      | 0.5     | 50%        |
| 1/4      | 0.25    | 25%        |
| 3/4      | 0.75    | 75%        |
| 1/10     | 0.1     | 10%        |
| 1/5      | 0.2     | 20%        |
| 3/10     | 0.3     | 30%        |
| 2/5      | 0.4     | 40%        |
| 3/5      | 0.6     | 60%        |
| 7/10     | 0.7     | 70%        |
| 4/5      | 0.8     | 80%        |
| 9/10     | 0.9     | 90%        |
| 1/100    | 0.01    | 1%         |
| 2/100    | 0.02    | 2%         |
| 3/100    | 0.03    | 3%         |
| 4/100    | 0.04    | 4%         |
| 5/100    | 0.05    | 5%         |

# Examples of SATs questions



#### Area, Perimeter and Volume

#### Area:

Area is the amount of space covered by a 2d shape. Area of a rectilinear shape (square, oblong) is calculated by the formula length x width. The area of a compound shape can be calculated by splitting the shape into its constituent parts, calculating their area and then adding them back together.



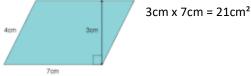
Assuming these are in cm 3 cm x 5 cm = 15 cm<sup>2</sup>

Area of a triangle is calculated by the formula (base x height)  $\div 2$ 



 $(12cmx20cm) \div 2 = 120cm^{2}$ 

Area of a parallelogram is calculated by the formula base x height.



Perimeter is the total outside length of sides of a shape added together

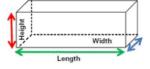
So the perimeter for this shape would be 16cm as the two longer sides are 5cm and the two shorter sides are 3cm.



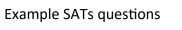
Volume is the internal space of a 3d object (i.e. how much it could contain). It is calculated by the formula length x width x height.

So if h = 3cm, width = 2cm and I = 6cm the volume

Volume = Length (L) × Width (W) × Height (H) would be:



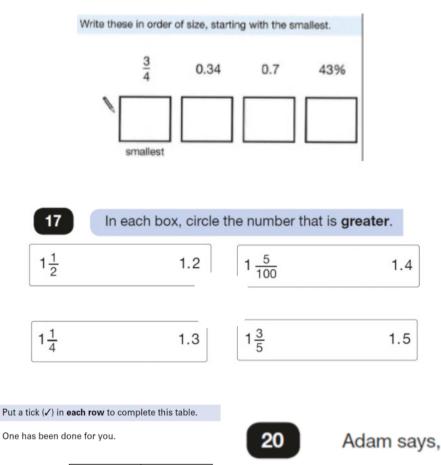
 $3 \times 2 \times 6 = 36 \text{ cm}^3$ 

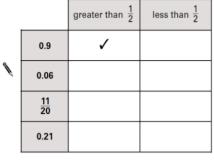


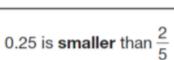
17

 $1\frac{1}{2}$ 

 $1\frac{1}{4}$ 







# Explain why he is correct.

Fractions Pointers

When **simplifying fractions,** find a common factor for the numerator and denominator then (to simplify as far as possible) use:

"Whatever I do to the bottom, I must do to the top" .

When **converting an improper fraction to mixed number** divide the denominator into the numerator. The whole number will give you the 'whole' part of the mixed number, any remainders should be put over the original denominator as a fraction (and then simplified if needed).

Adding or subtracting fractions—the denominators MUST be the same. Convert using common multiples and "Whatever I do to the bottom, I must do to the top".

Dividing fractions—remember 'Keep, change, flip' - KCF

**Multiplying fractions by whole numbers**— put a fraction line and 1 underneath the whole number and complete the calculation—multiply the numerators then multiply the denominators

When ordering fractions—convert all so they have the same denominator to make it easy to put them in order but remember to write the original fraction in the answer boxes.

# **Example SATs questions**

At the end of a film, the year is given in Roman numerals.



Write the year MMVI in figures.

Here is a number written in Roman numerals.

CXV

Write the number in figures.

# Example SATs questions

| Arabic Numeral | Roman Numeral |
|----------------|---------------|
| Arabic Numeral | Roman Num     |

| 1    | I    |
|------|------|
| 2    |      |
| 2    |      |
|      |      |
| 4    | IV   |
| 5    | V    |
| 6    | VI   |
| 7    | VII  |
| 8    | VIII |
| 9    | IX   |
| 10   | Х    |
| 20   | XX   |
| 30   | XXX  |
| 40   | XL   |
| 50   | L    |
| 60   | LX   |
| 70   | LXX  |
| 80   | LXXX |
| 90   | XC   |
| 100  | С    |
| 500  | D    |
| 1000 | М    |

|    | Circle th       | e fraction                        | that is gre    | ater than      | $\frac{1}{2}$ but less | s than <del>3</del> |               |
|----|-----------------|-----------------------------------|----------------|----------------|------------------------|---------------------|---------------|
|    |                 |                                   | 9              |                | 2                      | 4                   |               |
|    | ľ               | <u>7</u><br>8                     | 2 5            | <u>1</u><br>3  | 58                     |                     | 3             |
|    | $\frac{4}{6}$ × | $\frac{3}{5} =$                   |                |                | $\frac{5}{8}$ ÷        | 2 =                 |               |
|    | Two of the      |                                   | below are e    | quivalent.     |                        |                     |               |
|    | Circle the      | 2111.                             |                |                |                        |                     |               |
|    | ľ               | <u>2</u><br>3                     | <u>6</u><br>10 | <u>9</u><br>12 | <u>10</u><br>15        | <u>16</u><br>20     |               |
| In | this circle,    | $\frac{1}{4}$ and $\frac{1}{6}$ a | are shaded.    | Write the      | se fractions in        | order of siz        | e starting wi |

smallest.

 $\frac{3}{4}$ 

smallest

What fraction of the whole circle is not shaded?

| <u>3</u> | <u>9</u> | <u>17</u> |
|----------|----------|-----------|
| 5        | 10       | 20        |
|          |          |           |

Units of Measurement

# Example SATs questions

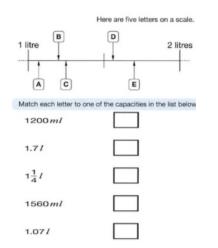
#### <u>Metric</u>

| Length/Distance | Weight/Mass       | Volume        |
|-----------------|-------------------|---------------|
| 1km = 1000m     | 1 tonne = 1000kg  | 1L = 1000ml   |
| 1m = 100cm      | 1kg = 1000g       | 1L = 100cl    |
| 1cm = 10mm      |                   | 1cl = 10ml    |
| 1m = 1000mm     |                   |               |
| 1/2 km=500m     | 1/2 tonne = 500kg | 1/2L = 500ml  |
| 1/2 m = 50cm    | 1/2kg = 500g      | 3/4L = 750ml  |
| 1/2/cm = 5mm    | 3/4 kg = 750g     | 1/4 L = 250ml |
| 3/4 km = 750m   | 1/4 kg = 250g     |               |
| 3/4 m = 75cm    |                   |               |
| 3/4 cm = 7.5mm  |                   |               |
| 1/4/km = 250m   |                   |               |
| 1/4 m = 25cm    |                   |               |
| 1/4 cm = 2.5mm  |                   |               |
|                 |                   |               |
| Imperial        |                   |               |

1 stone = 14 pounds (lb)

1 lb = 16 ounces (oz)

1 gallon = 8 pints



A bottle contains 568 millilitres of milk.



Amir has three parcels.

# Parcels A and B together weigh the same as parcel C.

The three parcels weigh 800 grams altogether.

Parcel A weighs 250g.

How much does parcel B weigh?

Metric/Imperial conversion (rough)

2.5cm = 1 inch

1 mile = 1760 yards

1 yard = 3 feet 1 foot = 12 inches

8km = 5 miles

500g = 1lb